



Development of a 25-DOF Hand Forward Kinematic Model Using Motion Data

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Global Contributor to Eco-Techno-Humanopia

Agenda







Ergonomic Design with Digital Hand Models

□ Hand-held device development in digital environment



Cell phone



Car interior design



Helicopter controller

Benefits

- Better fit to the grip posture
- Easily evaluate physical workloads such as grip force & torque
- Reduce the number of physical prototypes
- Reduce development time





Digital Hand Kinematic Modeling

Three key issues











Hand Link Length Estimation

Two-step Procedure

- S1. Determine joint center of rotation (COR)
- S2. Calculate link length (distance between adjacent joint CORs)
- Existing joint COR estimation method
 - Buchholz et al. (1992)
 - > Method
 - Attach markers to the fingers
 - Capture 3 or 4 X-ray images of the movement trajectory of makers
 - Estimate joint COR based on the trajectory
 - Do regression analysis based on 6 cadaver hands to derive the relation between hand link length (HLL) & hand length (HL): HLL = 0.32 HL ($R^2 = 0.43$)
 - Limitations
 - Limited number of X-ray images used
 - Small sample size (6 hands), R² value





Objectives of the Study

- Development of an optimization-based method for hand link length (HLL) estimation using 3D motion data collected by an optoelectronic motion capture system
- Development of a 25-DOF hand forward kinematic model for product design based on estimated HLL
- Evaluation of the model using motion data by comparing with SANTOSTM hand model which applies regression equations proposed by Buchholz et al. (1992) to estimate HLL





Hand Forward Kinematic Model Development

Three-step procedure to develop the model

S1: Identification of joint DOFs

(1) literature survey

(2) experimental identification

S2: Estimation of hand link lengths

- (1) motion data analysis
- (2) joint CORs estimation
- (3) hand link lengths calculation

S3: Application of forward kinematic algorithm

Denavit-Hartenberg method application





S1: Joint DOF Identification

□ Survey of joint DOF

Joints	Fingers				Wrist	Tatal	
	Thumb	Index	Middle	Ring	Little	Joint	Total
Carpometacarpal (CMC)	2[3*] (3)						
Metacarpophalangeal (MCP)	2[1**](2)	2	2	2	2		
Interphalangeal (IP)	1					2(3)	22(25)
Proximalinterphalangeal (PIP)		1	1	1	1		
Distalinterphalangeal (DIP)		1	1	1	1		

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*Buchholz, 1989; **JackTM (): DOF of the new model

- □ Feature of the new model
 - Comprehensive DOFs (25 totally)





S2: Hand Link Length Estimation

Assumption

- Rigid linkage representation of the hand
- Spherical trajectory of marker movement around joint COR
- Optimization routine
 - Cost function: variation of hand link length and depth from marker to joint COR during entire grip motion

$$C_{i} = \sum_{t=1}^{T} \left\{ \sum_{k=0}^{3} \left\| \left\| \vec{l}_{i,k}(t) \right\| - \left\| \vec{l}_{i,k} \right\| \right\}^{2} + \sum_{m=0}^{4} \left\| \left\| \vec{D}_{i,m}(t) \right\| - \left\| \vec{D}_{i,m} \right\| \right\}^{2} \right\}$$



S3: Forward Kinematic Method Application

- Denavit-Hartenberg method provides the transformation relationship between joint angles and fingertip position.
- □ Forward kinematic method predicts fingertip position, given joint angles

 $\mathbf{P} = f(\Theta)$

P: Fingertip Position, Θ: Joint Angles





Proposed Hand Forward Kinematic Model

- □ Input: joint angles
- Output: fingertip position





Experimental Evaluation







Participants



□ Five right-handed male participants

Classification	Mean (SD)	Range		
Age (years)	26.3 (2.1)	23~28		
Hand length (mm)	192 (10.1)	178~206		

□ Selection criteria

• No history of injuries at the hand and wrist





Apparatus

- Optoelectronic motion capture system: 6 Hawk Digital Cameras[®] (Motion Analysis Corporation, CA, USA)
- □ 24 spherical retro-reflective markers
 - Diameter: 5 mm



Motion capture system layout



Surface marker set





Joint Angle Calculation: 1 DOF

□ Flexion-extension angle of PIP joint

$$\theta = \arccos\left(\frac{\vec{a} \cdot \vec{b}}{\left|\vec{a}\right| \left|\vec{b}\right|}\right)$$





Joint Angle Calculation: 2 DOF

□ Flexion-extension and abduction-adduction angles of MCP joint





Evaluation Criteria

Prediction Error

• Distance between the measured fingertip position (X_M, Y_M, Z_M) and predicted fingertip position (X_P, Y_P, Z_P)

Prediction error =
$$\sqrt{(X_P - X_M)^2 + (Y_P - Y_M)^2 + (Z_P - Z_M)^2}$$

Unit: mm

Douticipanta	Classification	Index finger position				
Participants	Classification	X	Y	Z		
P1	Measured	-8.2	-39.3	128.8		
	Predicted	-7.8	-41.3	130.5		
	Prediction eror	2.7				





Evaluation Result

Fingertip prediction error at each finger Proposed model: Middle > Ring > Index > Little SANTOSTM hand model: Middle > Little > Ring > Index

Grand mean: Proposed model (2.7 mm) < SANTOSTM hand (5.8 mm)

Mean (SD) value (mm) of fingertip position prediction error

Hand model	Index	Middle	Ring	Little	Maximum
Proposed	2.2	3.6	3.1	1.8	9.7 (Middle)
Model	(2.5)	(3.2)	(2.8)	(1.5)	
SANTOS TM	5.4	6.3	5.7	5.9	15.3 (Middle)
Hand model	(3.2)	(3.7)	(1.5)	(1.3)	



Discussion

- The new hand model predicts fingertip position more accurate than SANTOSTM hand (2~3 mm on average).
- Accuracy of proposed optimization-based HLL estimation method > regression equations proposed by Buchholz et al. (1992)
- □ The model has lower accuracy at middle and ring fingers
 - Smaller amount of joint rotation for middle and ring fingers during ball grasping motion
 - More amount of joint rotation leads to more accurate estimation of HLL
- □ Source of prediction error
 - Attaching location of markers: need to locate markers right over the joint COR







Thank you!



